# Connecting the Dots

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#### Lessons from



### Geometry Labs Henri Picciotto (free download at www.MathEducationPage.org)



#### Find geoboard shapes with area 15

Find as many geoboard squares of different sizes (and their areas) as you can.

Hint: there are more than 10



#### What is the area of the red square?

outer square: 
$$6^2$$
  
each triangle:  $\frac{2 \cdot 4}{2} = 4$   
inner square:  $36 - 4 \cdot 4 = 20$ 

#### Generalize



outer square: 
$$(a + b)^2$$
  
each triangle:  $\frac{a \cdot b}{2}$   
inner square:  $(a + b)^2 - 2ab = a^2 + b^2$ 



Area of squares				
Small	Medium	Large		
~				
-				
~ 2				



Area of the red square: 20 Area of the green square: 5 Side of the red square:  $\sqrt{20}$ Side of the green square:  $\sqrt{5}$ Conclusion:  $\sqrt{20} = 2\sqrt{5}$  !

Simplify:  $\sqrt{147}$ 



$$\sqrt{147} = \sqrt{49.3} = 7\sqrt{3}$$

# Distance to the origin

1. What is the distance from each geoboard peg to the origin? Write your answers in simple radical form on the figure below.

•	٠	٠	٠	٠	٠	٠	٠	٠	٠	٠
•	•	•	•	•	•	•	•	•	•	•
•	•	•	•	•	•	•	•	•	•	•
•	•	•	•	•	•	•	•	•	•	•
•	•	٠	•	•	•	٠	٠	•	•	•
•	•	•	•	•	•	•	•	•	•	•
•	•	٠	•	•	•	٠	٠	•	•	•
•	•	•	•	•	•	•	•	•	•	•
•	•	$2\sqrt{2}$	•	•	•	•	•	•	•	•
•	$\sqrt{2}$	•	•	•	•	•	•	•	•	•
•	• 1	٠	•	•	•	٠	٠	•	٠	٠

#### Discussion

- **A.** Discuss any patterns you notice in the distances. Use color to highlight them on the figure. In particular, refer to the following features.
  - **a.** Symmetry
  - **b.** Slope

#### Similarity

Dilation (3,4) $\rightarrow$ (6,8) (5,3) $\rightarrow$ (10,6) (5,4) $\rightarrow$ (10,8)



Sides are proportional Angles are equal

#### Similar Rectangles



Sides are proportional

The diagonal test

There are ten families of similar rectangles on the geoboard. (with more than one rectangle per family)

Find them all.

## Slope

# Find all geoboard slopes between 1 and 2 (expressed as fractions and decimals).

Find all geobard slopes between 0.5 and 1.

## Extensions

#### Pick's Formula

1	•	•	7
• \	•	•/	•
•	\• ,	/•	•
•	V	•	•

Inside dots	Bound. dots	Area
9		



#### GEOBOARD DIAGONALS

If you connect (0, 0) to (5, 3) with a straight line, you go through seven unit squares.



14. Exploration If you connect (0, 0) to (p, q)with a straight line, how many unit squares do you go through? Experiment and look for patterns. (Assume p and q are positive whole numbers.) Keep a record of your work. Using manipulatives does not guarantee the development of skills, but it can encourage reflection and discussion.

This makes difficult topics more accessible, and can lead to deeper understanding for all.

It is a useful complement to traditional and electronic approaches in all classes.

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