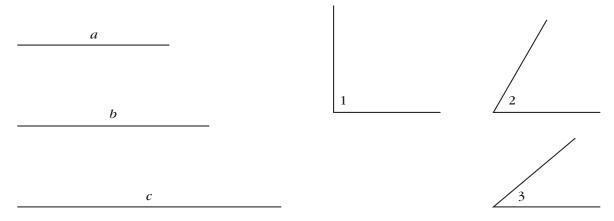
LAB 6.1 Noncongruent Triangles

Name(s)

Equipment: Compass, straightedge, unlined paper



Instructions: For the following problems,

- **a.** Use the compass and straightedge to construct *two noncongruent triangles* that satisfy the given conditions.
- **b.** Label the sides and angles that are equal to those shown above.
- **c.** If you cannot construct two noncongruent triangles, explain why, and construct just one triangle.
- d. If you cannot construct even one, explain why.
- **1.** One side of length *a* and an adjacent angle equal to $\angle 3$
- **2.** One side of length *a* and an opposite angle equal to $\angle 3$
- **3.** One angle equal to $\angle 1$ and one equal to $\angle 2$
- **4.** One angle equal to $\angle 1$, one equal to $\angle 2$, and one equal to $\angle 3$
- 5. One side of length *a*, one of length *b*, one of length *c*
- 6. One side of length a, one of length b, and between them an angle equal to $\angle 3$
- **7.** One side of length *a*, one of length *b*, and an angle equal to $\angle 3$ opposite the first side
- **8.** One side of length *a* between angles equal to $\angle 2$ and $\angle 3$
- **9.** One side of length *a* adjacent to an angle equal to $\angle 2$ and opposite an angle equal to $\angle 3$
- **10.** One side of length *a*, one of length *b*, one of length *c*, and an angle equal to $\angle 1$

Discussion

- **A.** Problem 1 could be described as an SA construction (one pair of equal sides and one pair of equal angles). Problem 6 could be described as an SAS construction (two pairs of equal sides with one pair of equal angles between them). Problem 7 could be described as an SSA construction (two pairs of equal sides with one pair of equal angles not between them). Make a two-column table to summarize your work in Problems 1–10.
 - In column 1, describe the problem using the letters S and A; each S represents a pair of equal sides, and each A represents a pair of equal angles.
 - In column 2, explain whether the given conditions lead to many possible triangles, two possible triangles, one possible triangle, or no triangles.
- **B.** Which problems had no solution? Why?
- **C.** Which problems had a unique solution? How can this help us recognize congruent triangles?
- **D.** Which problem had exactly two solutions?