Equipment: Compass, straightedge, unlined paper

c
Instructions: For the following problems,
a. Use the compass and straightedge to construct two noncongruent triangles that satisfy the given conditions.
b. Label the sides and angles that are equal to those shown above.
c. If you cannot construct two noncongruent triangles, explain why, and construct just one triangle.
d. If you cannot construct even one, explain why.

1. One side of length $a$ and an adjacent angle equal to $\angle 3$
2. One side of length $a$ and an opposite angle equal to $\angle 3$
3. One angle equal to $\angle 1$ and one equal to $\angle 2$
4. One angle equal to $\angle 1$, one equal to $\angle 2$, and one equal to $\angle 3$
5. One side of length $a$, one of length $b$, one of length $c$
6. One side of length $a$, one of length $b$, and between them an angle equal to $\angle 3$
7. One side of length $a$, one of length $b$, and an angle equal to $\angle 3$ opposite the first side
8. One side of length $a$ between angles equal to $\angle 2$ and $\angle 3$
9. One side of length $a$ adjacent to an angle equal to $\angle 2$ and opposite an angle equal to $\angle 3$
10. One side of length $a$, one of length $b$, one of length $c$, and an angle equal to $\angle 1$

## LAB 6.1 <br> Noncongruent Triangles (continued)

## Name(s)

## Discussion

A. Problem 1 could be described as an SA construction (one pair of equal sides and one pair of equal angles). Problem 6 could be described as an SAS construction (two pairs of equal sides with one pair of equal angles between them). Problem 7 could be described as an SSA construction (two pairs of equal sides with one pair of equal angles not between them). Make a two-column table to summarize your work in Problems 1-10.

- In column 1, describe the problem using the letters $S$ and $A$; each $S$ represents a pair of equal sides, and each $A$ represents a pair of equal angles.
- In column 2, explain whether the given conditions lead to many possible triangles, two possible triangles, one possible triangle, or no triangles.
B. Which problems had no solution? Why?
C. Which problems had a unique solution? How can this help us recognize congruent triangles?
D. Which problem had exactly two solutions?

